

# Recognition of digital fonts from images based on the disk cover

Mestetskiy Leonid ([mestlm@mail.ru](mailto:mestlm@mail.ru))

Lomov Nikita ([nikita-lomov@mail.ru](mailto:nikita-lomov@mail.ru))

Moscow State University  
Computational Mathematics and Cybernetics

# A lot of fonts

- The total number of Latin fonts - a few tens of thousands, and Cyrillic - twenty times less.



ИП-11. Barcelona, Spain

# Very wide variety of fonts

Aa Bb Cc Dd Ee Ff  
Gg Hh Ii Jj Kk Ll  
Mm Nn Oo Pp Qq  
Rr Ss Tt Uu Vv Ww  
Xx Yy Zz

ABCDEFGHIJKLM  
NOPQRSTUVWXYZ  
abcdefghijklm  
nopqrstuvwxyz

abcdefghijklmnopqrstuvwxyz

ABCDEFGHI  
JKLMNOPQ  
RSTUVWXY  
Z  
1234567890

AaBbCcDdEeFf  
GgHhIiJjKkLlMm  
NnOoPpQqRrSsTt  
UuVvWwXxYyZz  
1234567890@%&!?

ABCDEF  
GHIJKLMN  
OPQRSTU  
vwxyz

FreeFonts.Xyz

GHOULISH FRIGHT

ABCDEFGHIJ  
KLMNOPQR  
STUVWXYZ  
ABCDEFGHIJKLM  
NOPQRSTUVWXYZ  
0123456789

ABCDEF  
GHIJKLMN  
OPQRSTU  
vwxyz

FreeFonts.Xyz

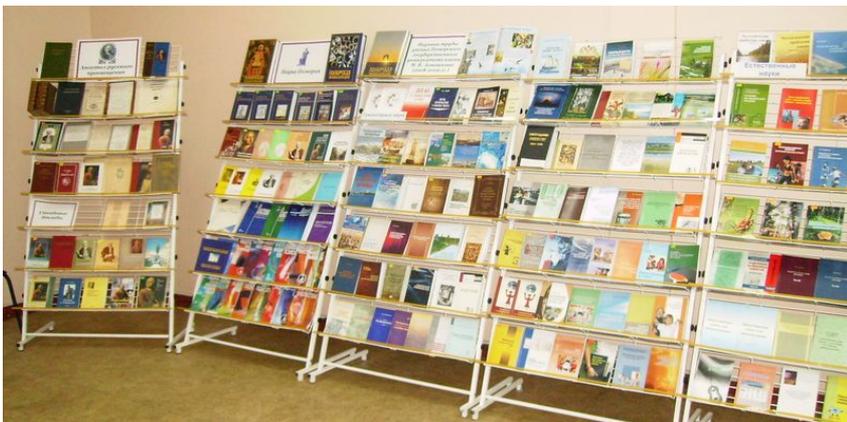
abcdefghijkl  
mnopqrs  
tuvwxyz  
hamburgerfons

ABCDEFGHIJ  
LMNOPQRST  
UVWXYZ

ABCDEF  
GHIJK  
LMNOP  
QRSTU  
vwxyz

# Fonts recognition problem

- Font Copyright Holder wants to control its use



# Fonts comparing problem

Designers want to choose a font similar to the sample available

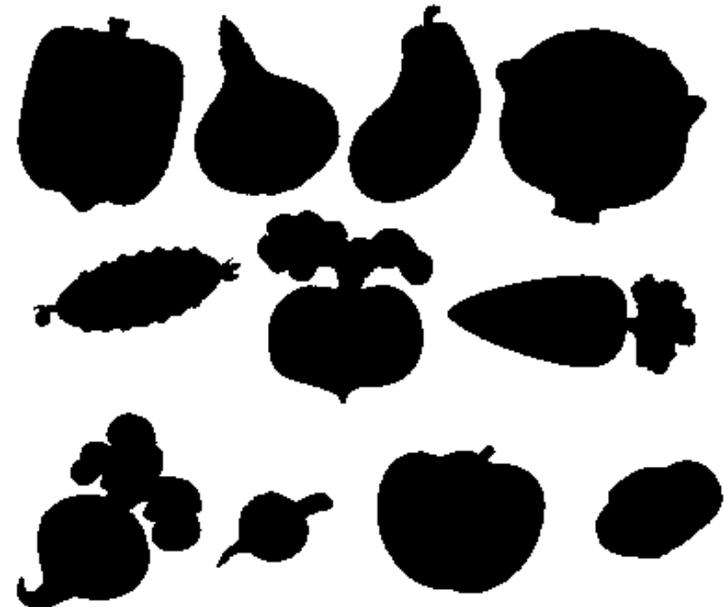
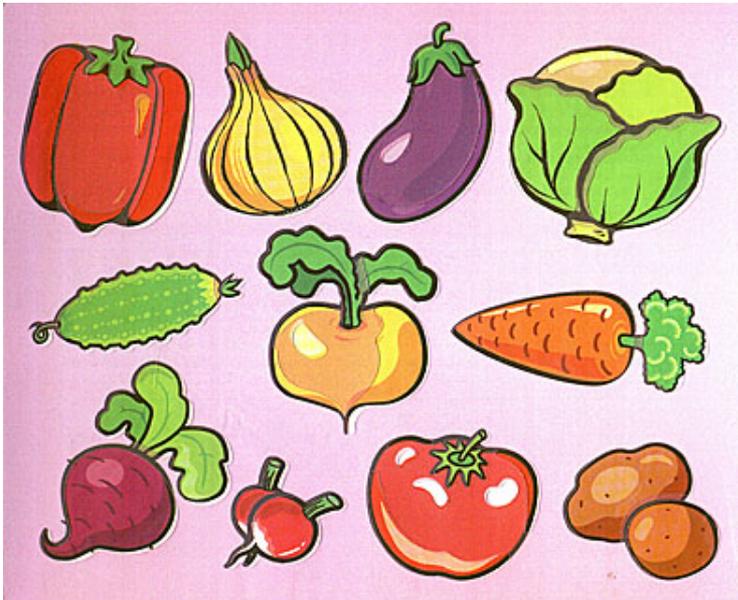
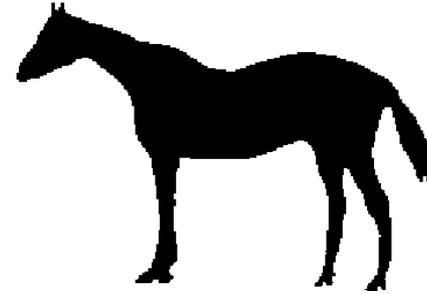


# Wanted a measure of the similarities and differences for digital fonts

## Requirements:

- The adequacy determining similarities and differences
- Universality for a variety of types, sizes, character sets
- The high computational efficiency for processing thousands of fonts

# A common problem - a comparison of shapes of objects



The shape - an external outline, external appearance of the object.

# The basic idea - to evaluate the area of the disk cover of the object

## Morphological width



Covering of the object by inscribed disks of different sizes

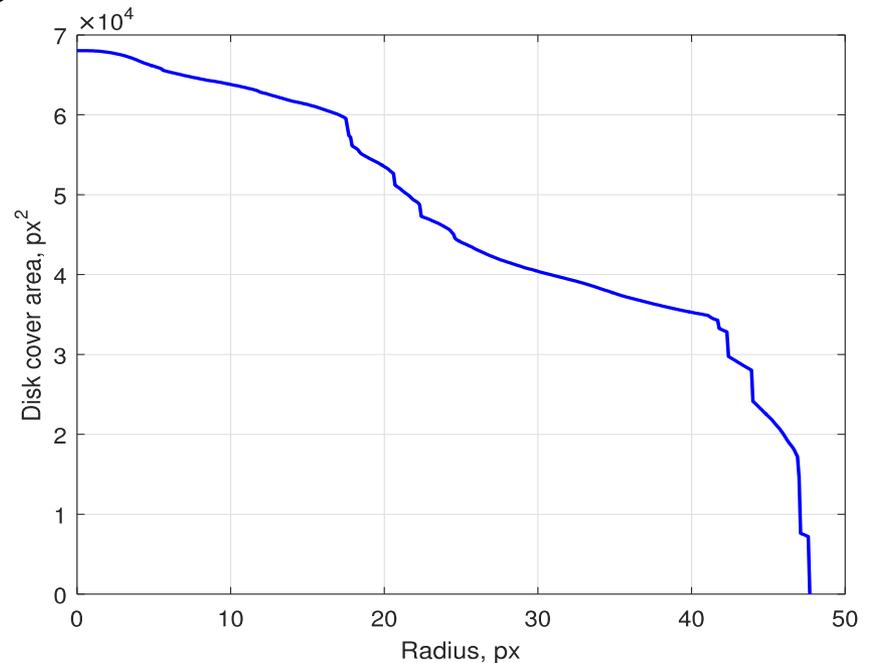
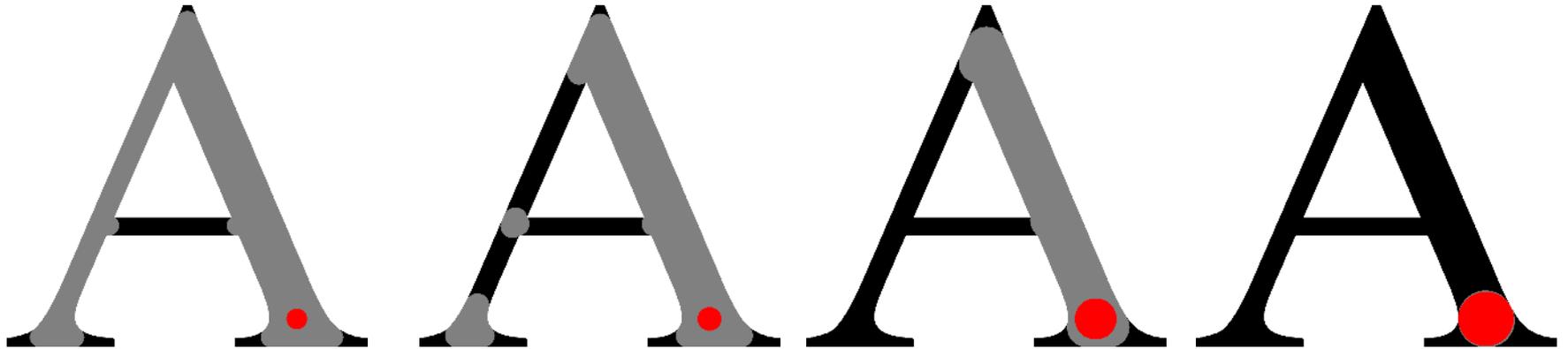
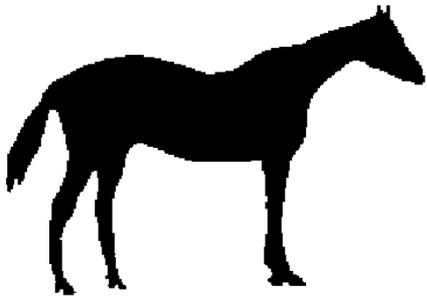


Diagram of disk cover area depending on the size of covering disc

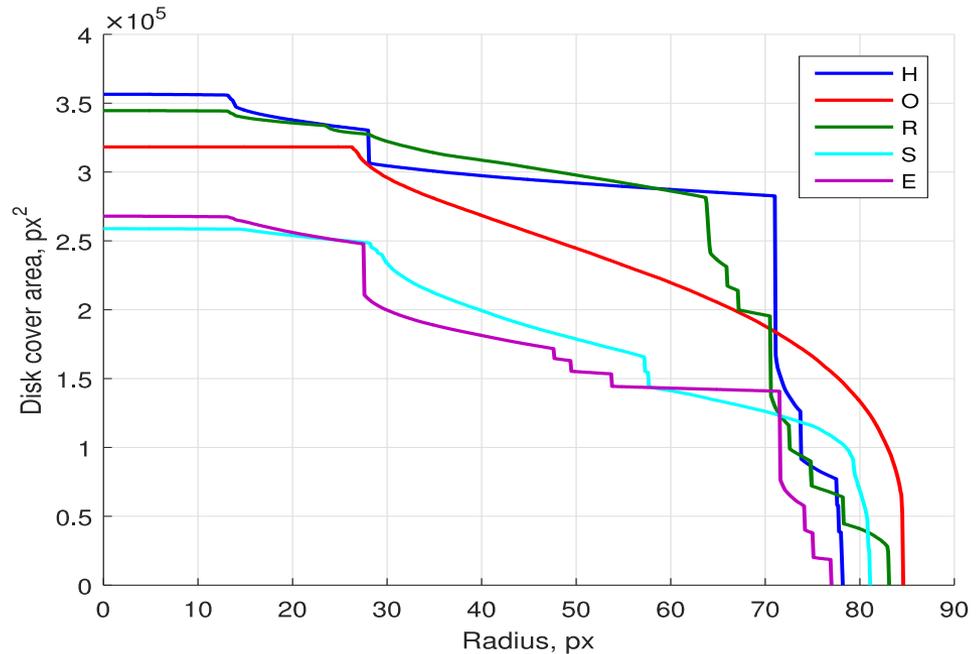
# Region of predetermined width



# Morphological width of the image is an informative feature



**HORSE**

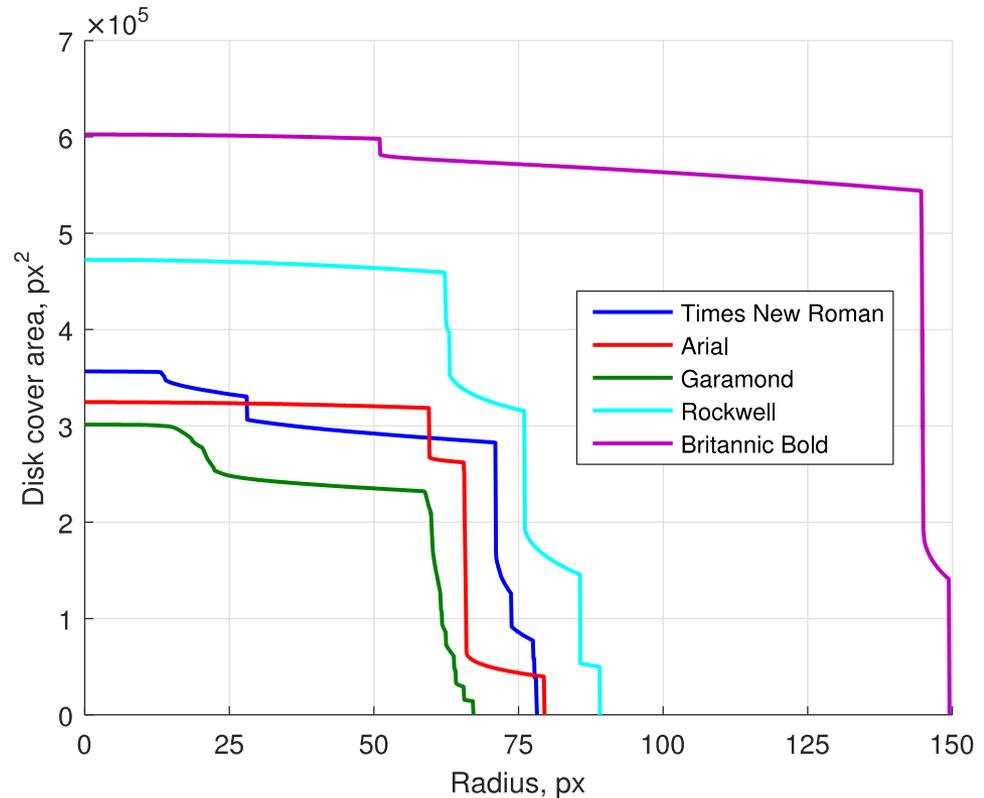


Morphological width of different characters  
of the same font

# Morphological width of fonts is the basis for comparison

HORSE  
HORSE  
HORSE  
HORSE  
HORSE

- Times New Roman
- Arial
- Garamond
- Britannic Bold
- Rockwell



Morphological width differentiates between fonts

# Font similarity measure based on morphological width

$$d(\mathbf{p}^k, \mathbf{q}) = \sum_{j=1}^n \alpha_j d_1(p_{c_j}^k, q_j).$$

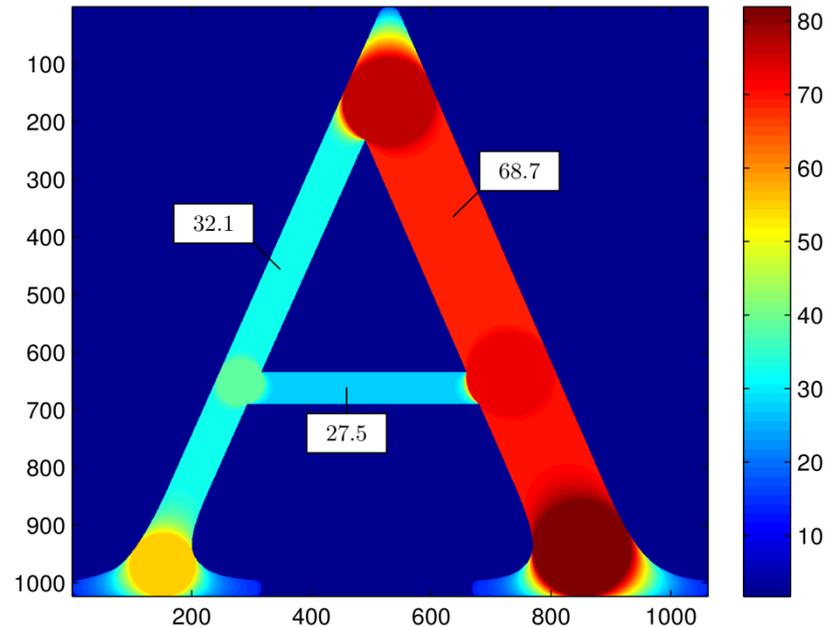
$c_j$  – код  $j$ -го символа шрифта

$p_{c_j}^k$  – эталонный дескриптор  $j$ -го символа шрифта  $\mathbf{p}^k$

$\mathbf{p}^k$  – шрифт

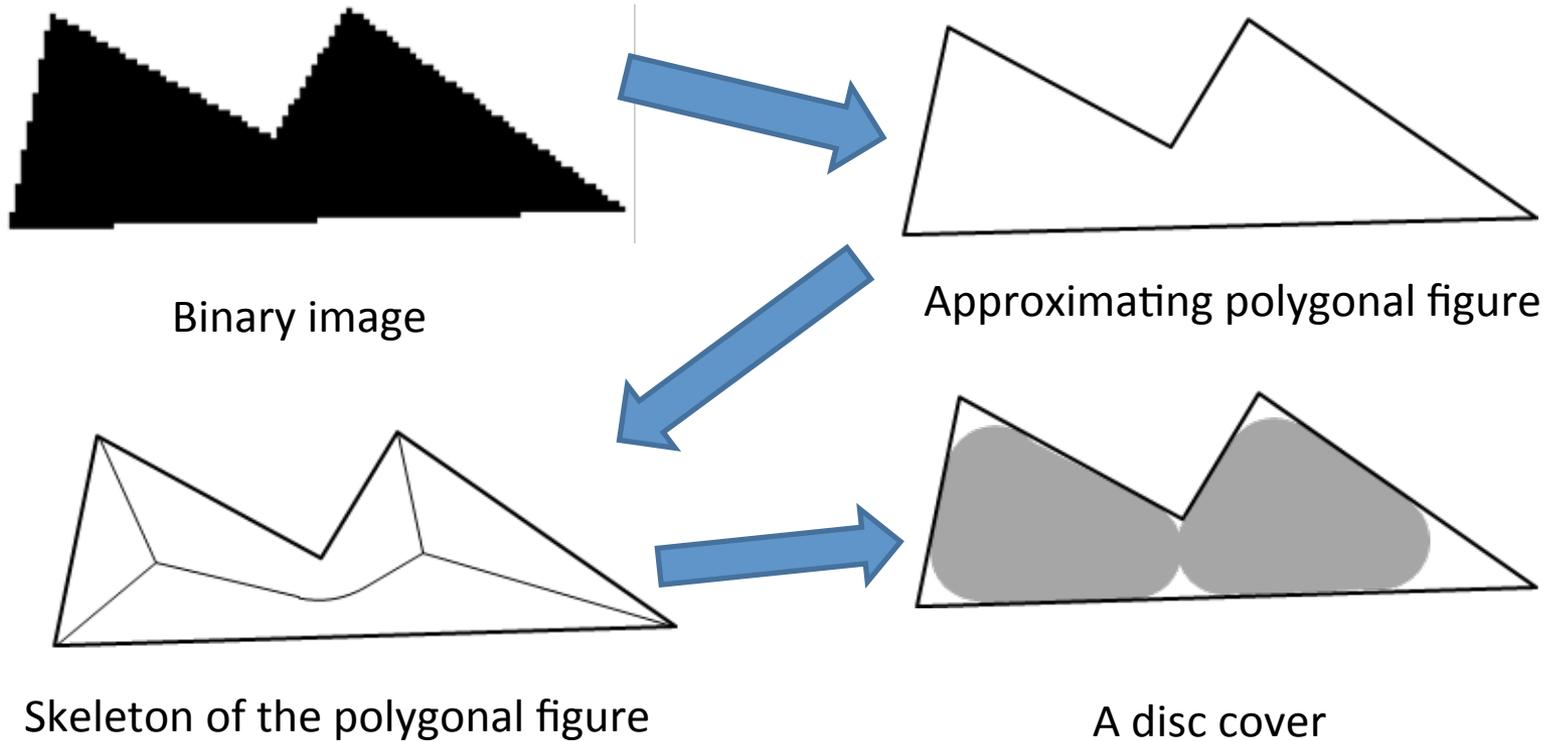
$\mathbf{q} = \{q_1, \dots, q_n\}$  – символы шрифта

# The problem of calculating of the disk cover area



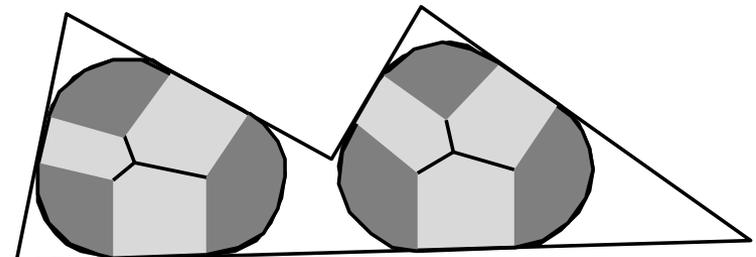
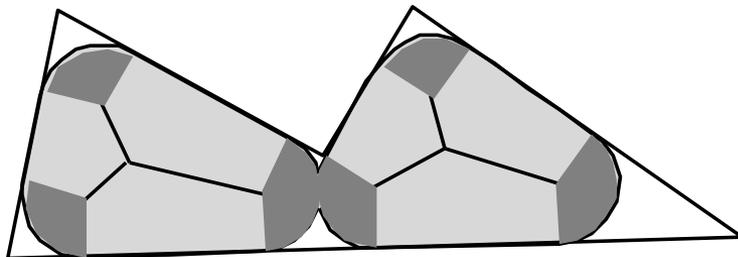
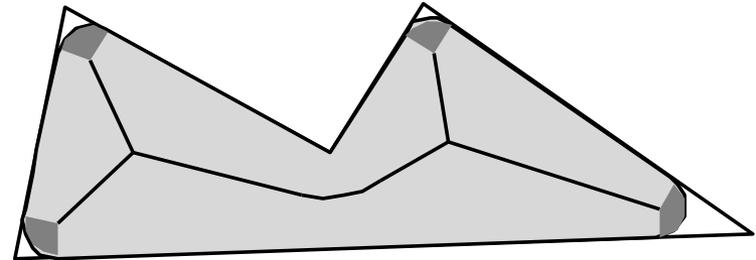
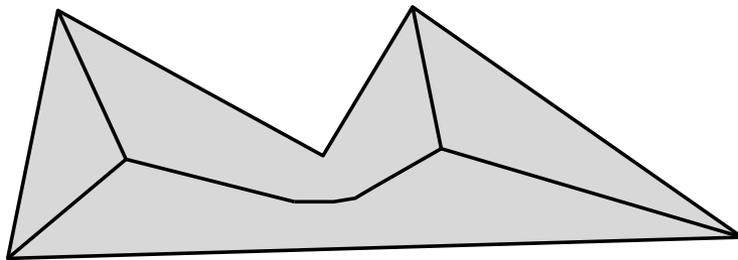
The main challenge - the development of efficient and accurate algorithm

# The idea of the proposed approach



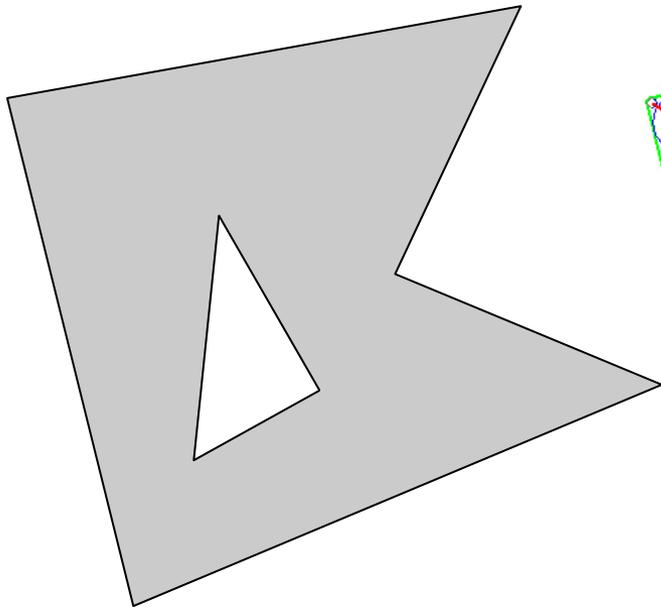
Continuous model of the disk cover for binary image

# Disk cover of polygonal figure

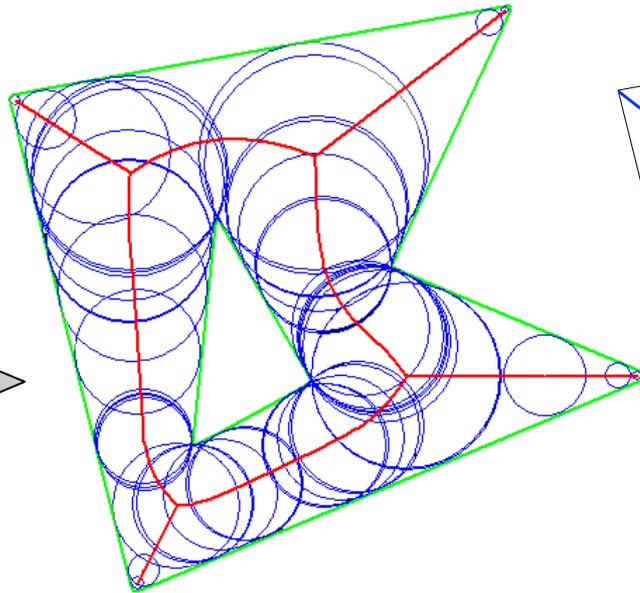


Changing of disk cover with increasing of disk size

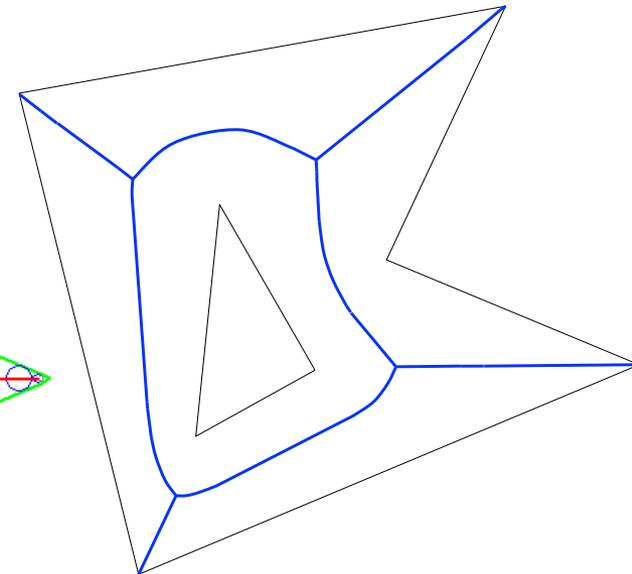
# Continuous medial representation of the polygonal figure



Polygonal figure



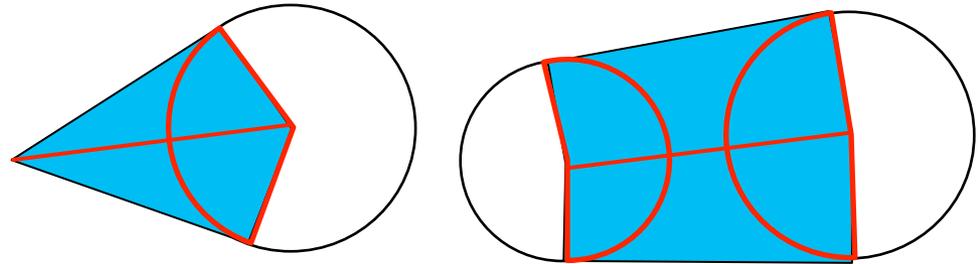
Medial representation  
(medial axis & radial function)



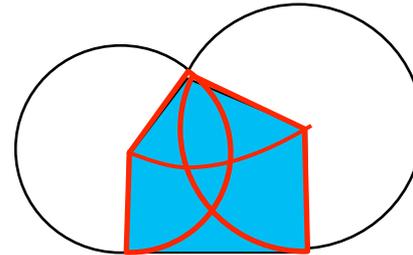
Skeleton

# Polygonal figures and bicircles

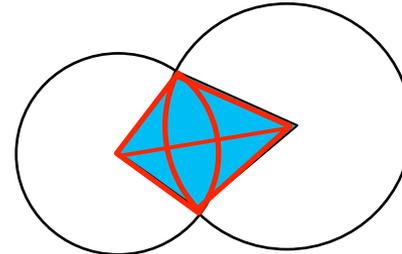
Lineare bicircles



Parabolic bicircles

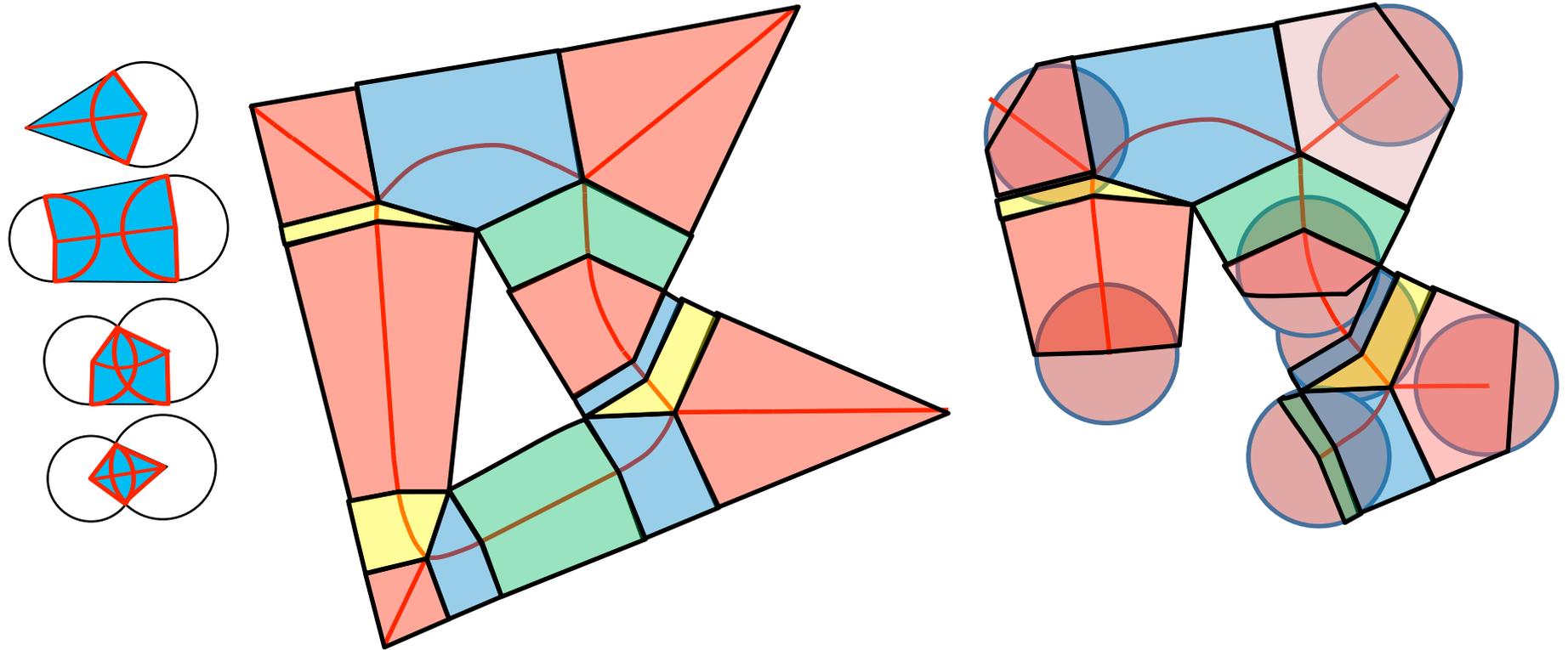


Hyperbolic bicircles



A bicircle is the union of all inscribed circles centered on one edge of the skeleton.

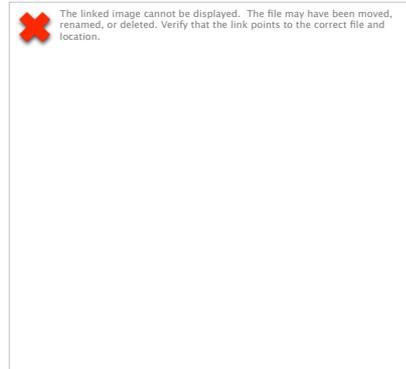
# Coverage of the figure by bicircles



All of the bicircles

Bicircles of given size

# Proper region and external sector



- $r, R$  – the radii of the smaller and larger end circles,
- $l$  – distance between centers of end circles,
- $t$  – the length of the projection of the bicircle axis to the segment-site,
- $S$  – area of the proper region of bicircle,
- $\varphi$  – the angular size of the external sector of bicircle.

# The calculation of the bicircle parameters

$$S_{lin} = 2 \cdot \frac{R+r}{2} \cdot t = (R+r) \cdot t$$

$$\varphi_{lin} = 2\alpha = 2 \cdot \arcsin \frac{t}{l}$$

}

Linear bicircle

$$S_{par} = \frac{R+r}{2} \cdot t + \sqrt{P(P-R)(P-r)(P-l)}$$

$$\varphi_{par} = \frac{\pi}{2} + \alpha = \frac{\pi}{2} + \arcsin \frac{p-r}{r}$$

}

Parabolic bicircle

$$S_{hyp} = 2\sqrt{P(P-R)(P-r)(P-l)}$$

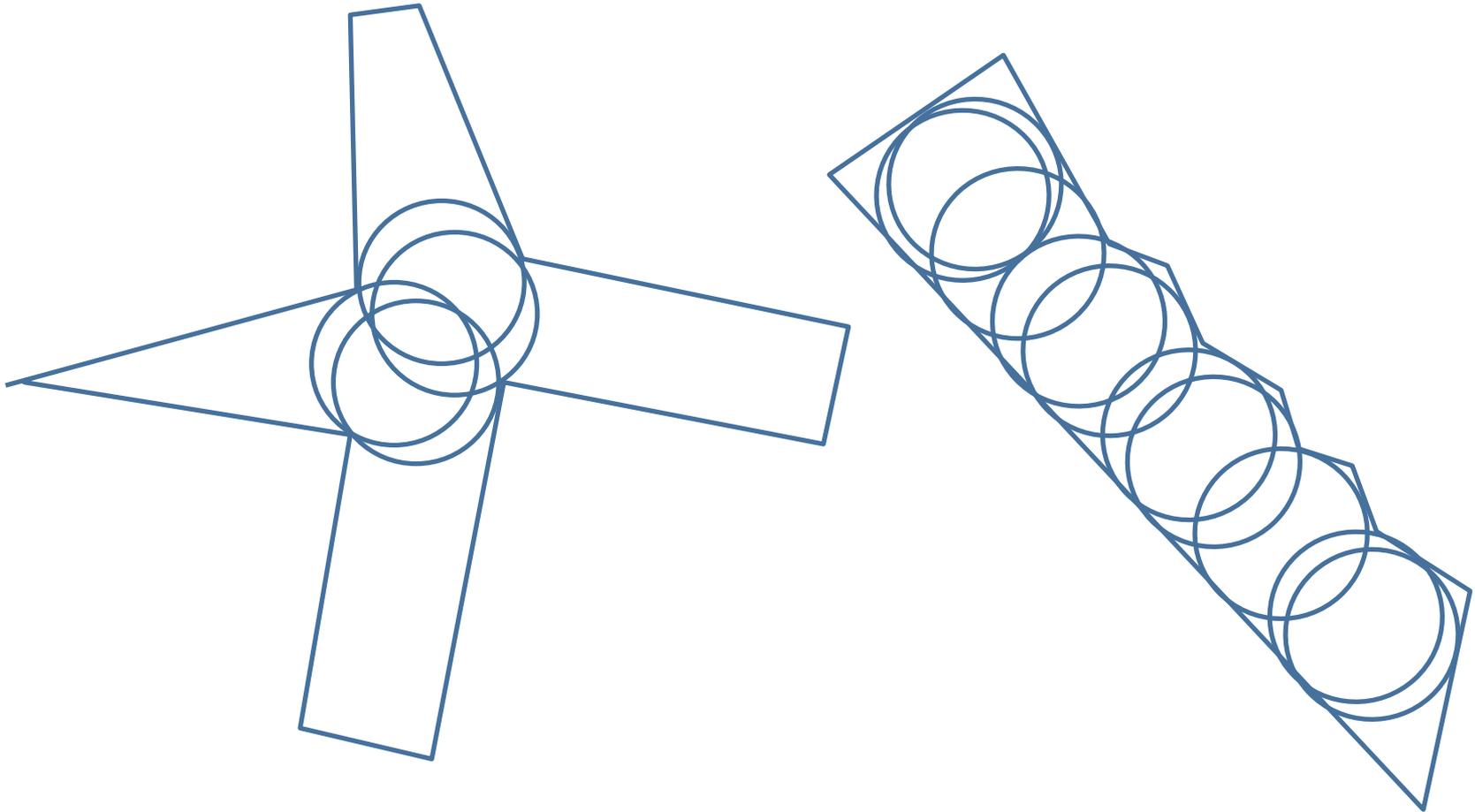
$$\varphi_{hyp} = 2\arcsin \frac{q}{2r}$$

}

Hyperbolic bicircle

$$P = (R+r+l)/2$$

# Bicircle overlapping problem



# Overlapping of bicircles



**Theorem.** *When we calculate the area of disk cover only pair crossing bicyclic should be considered (!!!)*



# Reference histograms - etalons

1884 fonts

52 glyphs (symbols)

5 font size (1000, 100, 50, 40, 30)

$1884 \times 52 \times 5 = 489840$  descriptors (4.2 hour, 11 min – polygon+skeleton+width)

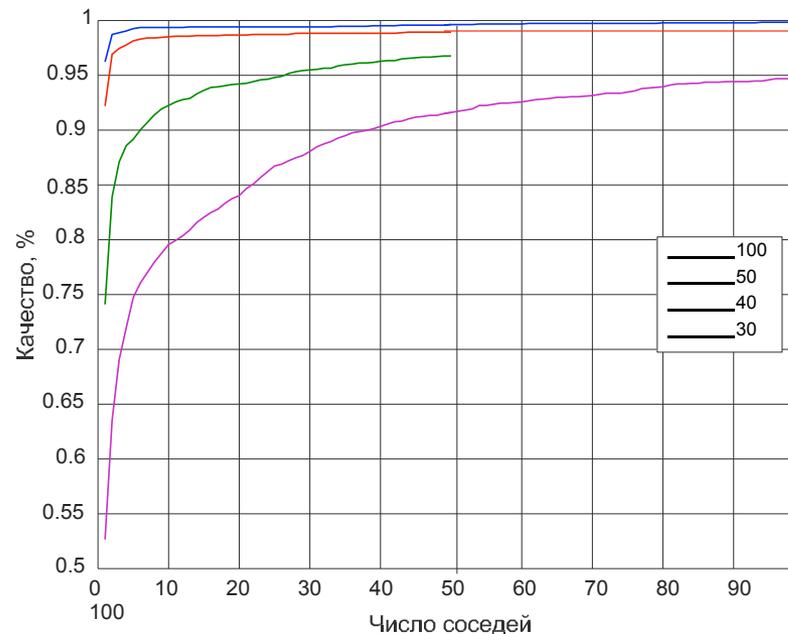
$1884 \times 1885 \times 52 = 184\,571\,712$  distances font-font (70 min – 2.25 sec/request)

Font Height	Running time, min	Time per glyph, sec
1000	192	0.118
100	25	0.015
50	14	0.009
40	12	0.007
30	9	0.006

# Experiment results

Размер	1	3	5	7
100	96.23%	98.89%	99.26%	99.36%
50	92.20%	97.45%	98.14%	98.41%
40	74.10%	87.10%	89.17%	90.71%
30	52.65%	69.06%	74.73%	77.07%

The percentage of hits in the number of nearest neighbors



# Conclusion

- The proposed descriptor and the method of its calculation open up new possibilities for the use of highly efficient computational geometry algorithms in image analysis and shape recognition.
- The proposed continuous model of width of polygonal figures on the basis of the disk cover allowed to make the decomposition of the original problem and reduce the computation to simple geometric calculations.
- The developed algorithm is the first to provide accurate analytical representation of the width distribution function of a polygonal figure.
- The high efficiency of the proposed method allows to compare and measure the similarity of figures by their width in real-time systems.
- The method successfully solves the problem of individual identification of the font on the real images of sufficient quality.

# Full description of the algorithm

Ломов Н.А., Местецкий Л.М.

Площадь дискового покрытия – дескриптор  
формы изображения

в журнале Компьютерная оптика, том 40,  
№ 4, с. 516-525